### 3.4 USING EXPONENTS TO SOLVE PROBLEMS

Name: $\qquad$
A lot of mathematical and scientific formula's and equations involve variables AND EXPONENTS!
For Example: $A=\pi r^{2} \quad a^{2}+b^{2}=c^{2} \quad x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a} \quad E_{k}=\frac{1}{2} v^{2}$
Now that you have practiced working with exponents you can apply your knowledge to a variety of practical problems.

## A) SOLVING WORD PROBLEMS WITH EXPONENTS

## Example \#1:

Mountain pine beetles can double their population in one year if conditions are right. They live in mature lodgepole and jack pine trees by boring into the bark. Only 5 mm long, these small beetles can kill pine trees if their numbers are great enough. Suppose the beetle population in a particular area is 10,000 and it doubles each year. What will the population be in 1 year? 2 years? 3 years?
a) Create a table to show the growth of the population of pine beetles over 3 years.

| a) Time (years) | a) Beetle population (\#) | b) |
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b) Express the population as a product of 10,000 and a power of 2 . Add this information to your table.
c) What patterns do you notice in your table?
d) Write an expression in exponential form to determine the number of beetles in n years. Explain what each part of the expression represents.

## B) THE PYTHAGOREAN THEOREM

The Pythagorean theorem states that for any RIGHT triangle, the length of the hypotenuse squared is equal to the sum of the squares of the other two sides.


This can be rearranged in different ways so you can solve for different sides:

| $a^{2}+b^{2}=\boldsymbol{c}^{2}$ |  |  |  |  |
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## Example 2:

Solve for the unknown side length:
a)

b)

64. The population of certain forms of bacteria double every day. If the population began with 1 million, how large would the population be after 7 days? Write your answer first as a power and then evaluate it.
65. Rory is 16 and just invested $\$ 1000$ in a mutual fund that should grow in value by $8 \%$ per year. At this rate his money will double every 9 years. How much will his initial investment be worth when he retires at age 61? Write your answer first as a power and then evaluate it.
66. The Richter scale represents a 10 -fold increase in intensity for every 1 unit of magnitude on the Richter scale. That means that a Richter scale rating of 2 is ten times more intense than a Richter scale rating of 1 . How much greater is a Richter scale rating of 8 compared to a Richter scale rating of 4 ? Write your answer first as a power and then evaluate it.

Using exponents and order of operations to solve problems.
155. Balkee invested $\$ 2000$ in a mutual fund that returned $8 \%$ interest each year. The following formula can be used to determine the answer. $A=\$ 2000(1.08)^{23}$. How large will the investment be in 23 years?
156. A colony of bees increases 2 fold every week. How large will the colony grow to after 20 weeks if it began with 2 bees. The following formula can be used to determine the answer. $A=2(2)^{20}$.
157. A very nosey student asked Mr. Spray how much he charges his tenants each month for rent. Mr. Spray gladly answered, "I charge them $0.15 \times 10^{4}$ dollars each month." How much does he charge his tenants each month and how weird is he?

A right triangle has two shorter sides that measure 8 cm and 15 cm .
What is the area of a square attached to the hypotenuse of the right triangle?


