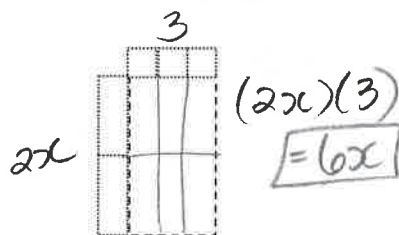
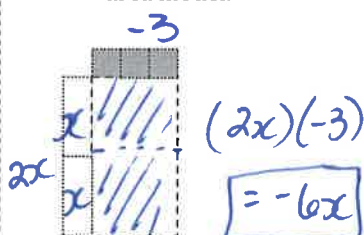


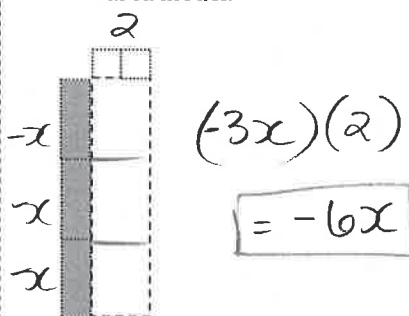
78. Write an equation represented by the diagram below and then multiply the two polynomials using the area model.



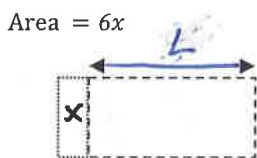
79. Write an equation represented by the diagram below and then multiply the two polynomials using the area model.



80. Write an equation represented by the diagram below and then multiply the two polynomials using the area model.



81. Write a quotient that can be represented by the diagram below and then find the missing side length using the area model.



Length: 6

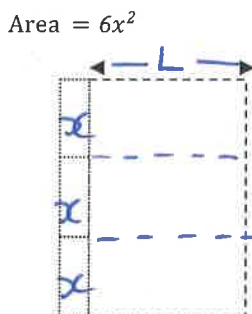
$$A = L \cdot W$$

$$\frac{6x}{x} = \frac{L \cdot x}{x}$$

$$\frac{6x}{x} = L$$

$$\boxed{\therefore L = 6}$$

82. Write a quotient that can be represented by the diagram below and then find the missing side length using the area model.



Length: 2x

$$A = L \cdot W$$

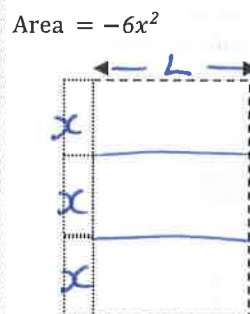
$$\frac{6x^2}{3x} = \frac{L \cdot 3x}{3x}$$

$$\therefore \frac{6x^2}{3x} = L$$

$$\therefore \frac{6x^2}{3x} = L$$

$$\boxed{2x = L}$$

83. Write a quotient that can be represented by the diagram below and then find the missing side length using the area model.



Length: -2x

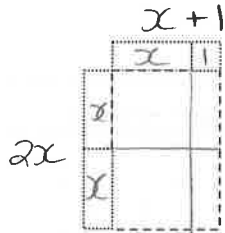
$$A = L \cdot W$$

$$\frac{-6x^2}{-2x} = \frac{L \cdot -2x}{-2x}$$

$$\boxed{1-2x = L}$$

class example.

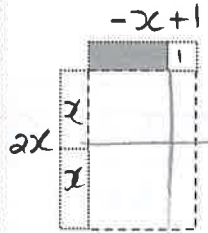
84. Write an equation represented by the diagram below and then multiply the two polynomials using the area model.



$$2x(x+1)$$

$$\boxed{2x^2 + 2x}$$

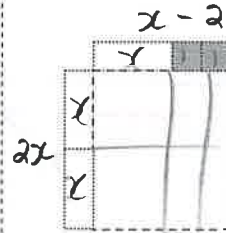
85. Write an equation represented by the diagram below and then multiply the two polynomials using the area model.



$$2x(-x+1)$$

$$\boxed{-2x^2 + 2x}$$

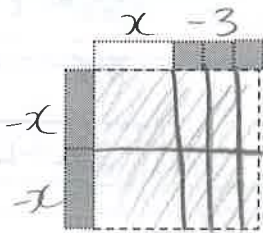
86. Write an equation represented by the diagram below and then multiply the two polynomials using the area model.



$$2x(x-2)$$

$$\boxed{2x^2 - 4x}$$

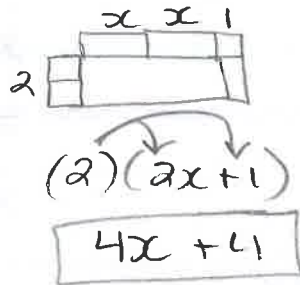
87. Write an equation represented by the diagram below and then multiply the two expressions using the area model.



$$-2x(x-3)$$

$$\boxed{-2x^2 + 6x}$$

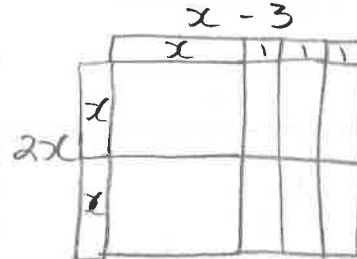
88. Draw and use an area model to find the product: $(2)(2x+1)$



$$(2)(2x+1)$$

$$\boxed{4x + 2}$$

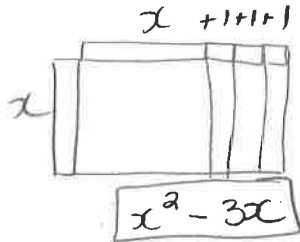
89. Draw and use an area model to find the product: $(2x)(x-3)$



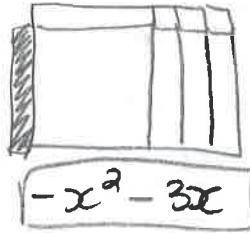
$$(2x)(x-3)$$

$$\boxed{2x^2 - 6x}$$

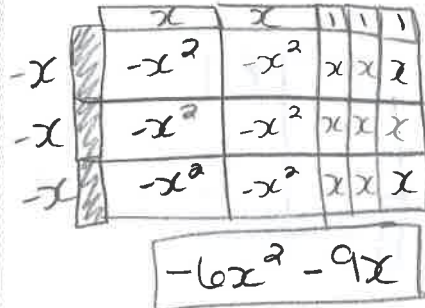
90. Draw and use an area model to find the product:
 $(x)(x + 3)$



91. Draw and use an area model to find the product:
 $(-x)(x + 3)$

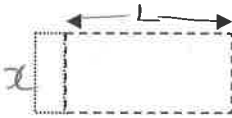


92. Draw and use an area model to find the product:
 $(-3x)(2x + 3)$



93. Write a quotient that can be represented by the diagram below and then find the missing side length using the area model.

Area = $x^2 + 3x$



$A = L \cdot w$

$$\frac{x^2 + 3x}{x} = \frac{L \cdot \cancel{x}}{\cancel{x}}$$

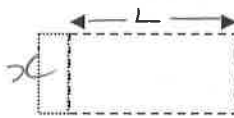
Length: $x + 3$

$$L = \frac{x^2 + 3x}{x}$$

$L = x + 3$

94. Write a quotient that can be represented by the diagram below and then find the missing side length using the area model.

Area = $-x^2 - 3x$



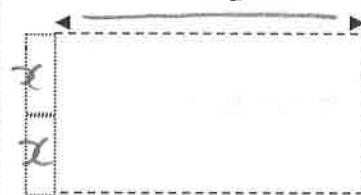
$A = L \cdot w$

$$\frac{-x^2 - 3x}{x} = \frac{L \cdot \cancel{x}}{\cancel{x}}$$

Length: $-x - 3$

95. Write a quotient that can be represented by the diagram below and then find the missing side length using the area model.

Area = $2x^2 - 8x$



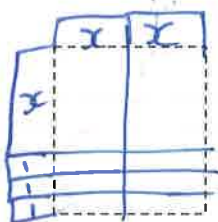
$A = L \cdot w$

$$\frac{2x^2 - 8x}{2x} = \frac{L \cdot \cancel{2x}}{\cancel{2x}}$$

Length:

$x^2 - 4$

96. Find the area, length and width that can be represented by the diagram.

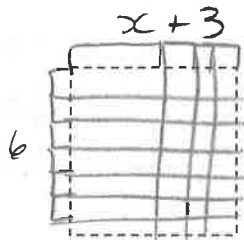


Area: $2x^2 + 6x$
 Length: $x + 3$
 Width: $2x$

$$2x(x+3)$$

$$2x^2 + 6x$$

97. Find the area, length and width that can be represented by the diagram.

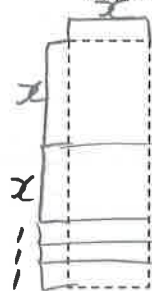


Area: $6x + 18$
 Length: 6
 Width: $x + 3$

$$6(x+3)$$

$$6x + 18$$

98. Find the area, length and width that can be represented by the diagram.



Area: $2x^2 + 3x$
 Length: $2x + 3$
 Width: x

$$x(2x+3)$$

$$2x^2 + 3x$$

Multiplying & Dividing Monomials without TILES

When multiplying expressions that have **more than one variable** or **degrees higher than 2**, algebra tiles are not as useful.

(monomial)(monomial)

Multiplying Monomials:

Eg.1.
 $(2x^2)(7x)$ Multiply numerical coefficients.
 $= 2 \times 7 \times x \times x^2$ Multiply variables using exponent laws.
 $= 14x^3$

Eg.2.
 $(-4a^2b)(3ab^3)$
 $= -4 \times 3 \times a^2 \times a \times b \times b^3$
 $= -12a^3b^4$

- ① Multiply coefficients
- ② Exponent laws.

Dividing Monomials:

Eg.1.
 $\frac{20x^3y^4}{-5x^2y^2}$
 ① Divide the numerical coefficients.
 $= \frac{20}{-5} \frac{x^3y^4}{x^2y^2}$
 ② Divide variables using "exponent laws."
 $= -4xy^2$

Eg.2.
 $\frac{-36m^3n^4p^2}{-9m^3np}$
 $= \frac{-36}{-9} \frac{m^3n^4p^2}{m^3np}$
 $= 4n^3p$

Revisit the exponent laws if...needed

$a^m \cdot a^n = a^{m+n}$
 $\frac{a^m}{a^n} = a^{m-n}$ | $(a^m)^n = a^{m \cdot n}$

Multiply or Divide the following.

99. $(-2ub^3)(-3ub^5)$
 $-2x-3 \times a \times a \times b^3 \times b^5$
 $= 6a^2b^8$

100. $(5x^2y^3)(-2x^3y^5)$
 $-10x^5y^8$

101. $4x(-3x^3)$
 $-12x^4$

102. $(\frac{1}{2}ab^2)(\frac{3}{4}a^3b)$
 $\frac{1}{2} \cdot \frac{3}{4} \cdot a \cdot a^3 \cdot b^2 \cdot b$
 $\frac{3}{8}a^4b^3$

103. $\frac{-75t^5}{15t^2}$
 $(-75 \div 15)t^{5-2}$
 $-5t^3$

104. $\frac{15x^3yz^2}{3x^2y}$
 $5xz^2$

105. $\frac{24x^3y^2}{18xy^3}$
 divide by HCF (6)
 $\frac{4}{3} \cdot x^{3-1} \cdot y^{2-3}$
 $\frac{4x^2}{3y}$
 * goes on bottom of fraction

106. $(2cd)(-2c^2d^3)(5c)$
 $2 \cdot -2 \cdot 5 \cdot c \cdot d \cdot c^2 \cdot d^3 \cdot c$
 $-20c^4d^4$

107. $\frac{(3xy)(4x^2y^2)}{12x^4y^3}$
 $\frac{12x^3y^3}{12x^4y^3}$
 $x^3y^3 / x^4y^3 = x^{-1}y^0 = \frac{1}{x}$
 $\frac{1}{x}$
 *Top 1st

* FOIL → First outside, inside last

(binomial)(binomial)

Multiplying Binomials

Challenge:

108. Which of the following are equal to $x^2 + 9x + 18$? → multiplies to 18, adds to 9
- a) $(x + 3)(x + 6)$
 - b) $(x + 1)(x + 18)$
 - c) $(x - 3)(x - 6)$
 - d) $(x + 2)(x + 9)$

Challenge:

109. Multiply $(2x + 1)(x - 5)$

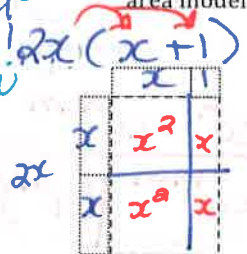
$$2x^2 - 10x + x - 5$$

$$2x^2 - 9x - 5$$

- ① Expand
- ② Combine Like Terms

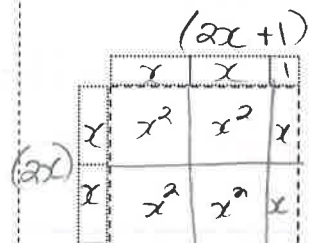
* Counting up the algebra tiles can help check your answer!!

110. Write an equation represented by the diagram below and then multiply the two polynomials using the area model.



$$2x^2 + 2x$$

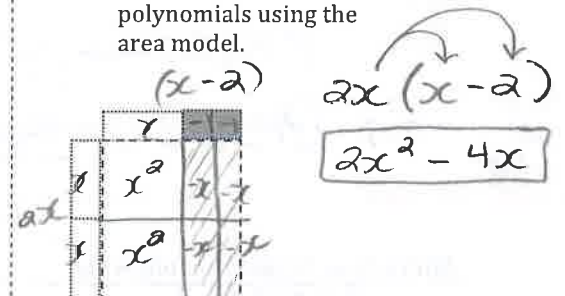
111. Write an equation represented by the diagram below and then multiply the two polynomials using the area model.



$$2x(2x + 1)$$

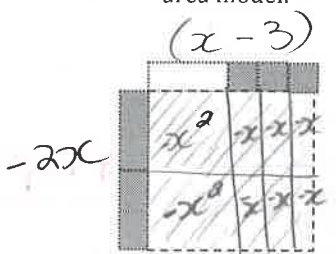
$$4x^2 + 2x$$

112. Write an equation represented by the diagram below and then multiply the two polynomials using the area model.



$$2x^2 - 4x$$

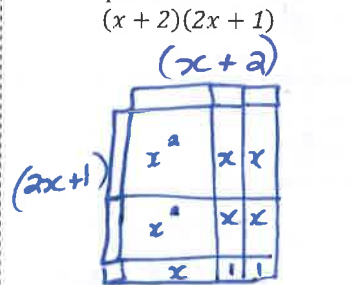
113. Write an equation represented by the diagram below and then multiply the two polynomials using the area model.



$$-2x(x - 3)$$

$$-2x^2 + 6x$$

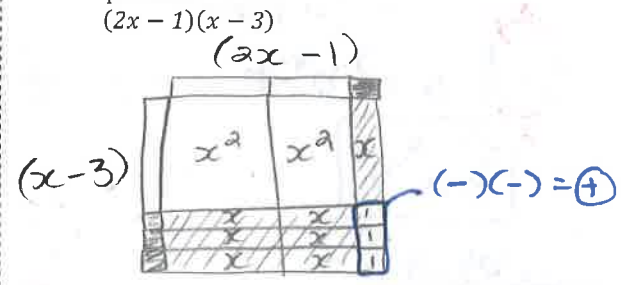
114. Draw and use an area model to find the product:



$$(2x + 1)(x + 2)$$

$$2x^2 + 5x + 2$$

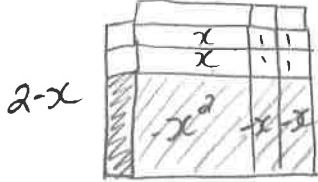
115. Draw and use an area model to find the product:



$$2x^2 - 7x + 3$$

116. Draw and use an area model to find the product:

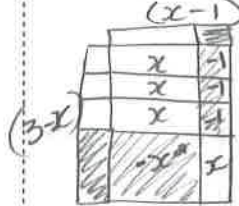
$$(2-x)(x+2)$$



$$-x^2 + 4$$

117. Draw and use an area model to find the product:

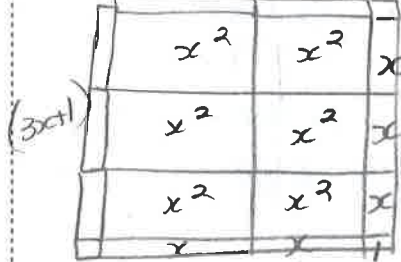
$$(3-x)(x-1)$$



$$-x^2 + 4x - 3$$

118. Draw and use an area model to find the product:

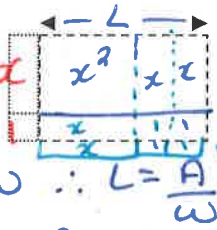
$$(3x+1)(2x+1)$$



$$6x^2 + 5x + 1$$

119. Write a quotient that can be represented by the diagram below and then find the missing side length using the area model.

$$\text{Area} = x^2 + 3x + 2$$



$$A = L \cdot w \therefore L = \frac{A}{w}$$

$$\frac{x^2 + 3x + 2}{x + 1} = L$$

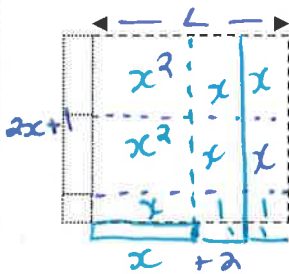
Length: $x+2$

$$(x+1)(x+2) = x^2 + 3x + 2$$

must add to $3x$ must multiply to get 2

120. Write a quotient that can be represented by the diagram below and then find the missing side length using the area model.

$$\text{Area} = 2x^2 + 5x + 2$$

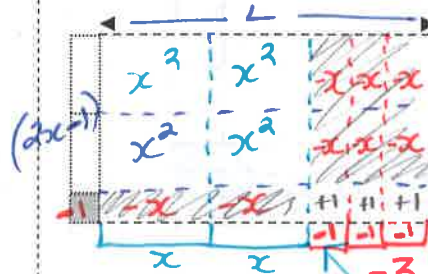


Length: $x+2$

$$(2x+1)(x+2) = 2x^2 + 5x + 2$$

121. Write a quotient that can be represented by the diagram below and then find the missing side length using the area model.

$$\text{Area} = 4x^2 - 8x + 3$$



Length: $2x-3$

$$(2x-1)(2x-3) = 4x^2 - 8x + 3$$

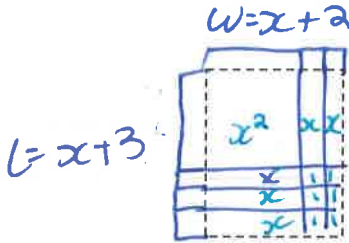
check.

Fit in $-8x$... also tells you that this must be -3

write in $4x^2$ tells you must be $x+x$ along side

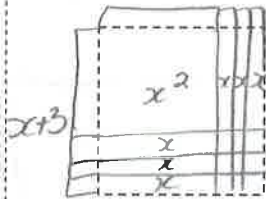
Various Answers.

122. Find the area, length and width that can be represented by the diagram.



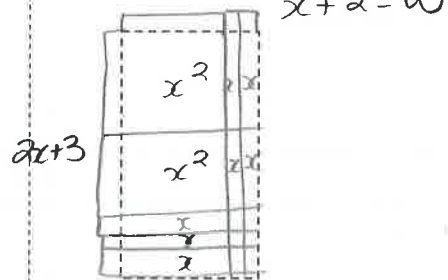
Area: $x^2 + 5x + 6$
 Length: $x + 3$
 Width: $x + 2$

123. Find the area, length and width that can be represented by the diagram.



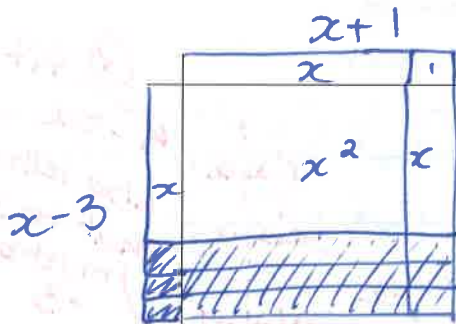
Area: $x^2 + 6x + 9$
 Length: $x + 3$
 Width: $x + 3$

124. Find the area, length and width that can be represented by the diagram.



Area: $2x^2 + 7x + 6$
 Length: $2x + 3$
 Width: $x + 2$

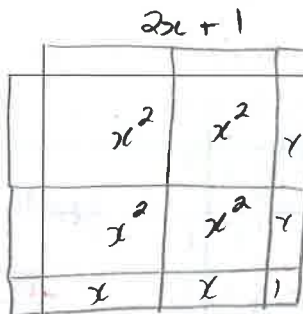
125. Draw tiles that represent the multiplication of $(x + 1)(x - 3)$.



What is the product of $(x + 1)(x - 3)$?

$x^2 - 3x + x - 3$
 $x^2 - 2x - 3$

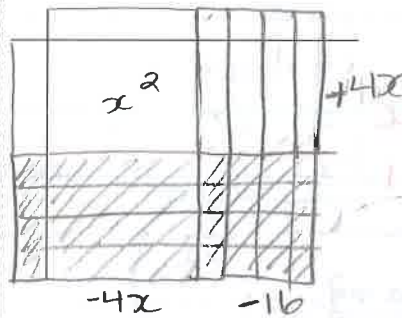
126. Draw tiles that represent the multiplication of $(2x + 1)(2x + 1)$.



What is the product of $(2x + 1)(2x + 1)$?

$4x^2 + 4x + 1$

127. Draw tiles that represent the multiplication of $(x - 4)(x + 4)$.



What is the product of $(x - 4)(x + 4)$?

$x^2 - 4x + 4x - 16$
 $x^2 - 16$